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Reliability block diagrams

Diagrammes de fiabilité

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INTERNATIONAL ELECTROTECHNICAL COMMISSION

RELIABILITY BLOCK DIAGRAMS

FOREWORD

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International Standard IEC 61078 has been prepared by IEC technical committee 56: Dependability.

This third edition cancels and replaces the second edition published in 2006. This edition constitutes a technical revision.

This edition includes the following significant technical changes with respect to the previous edition:

- a) the structure of the document has been entirely reconsidered, the title modified and the content extended and improved to provide more information about availability, reliability and failure frequency calculations;
- b) Clause 3 has been extended and clauses have been introduced to describe the electrical analogy, the "non-coherent" RBDs and the "dynamic" RBDs;
- c) Annex B about Boolean algebra methods has been extended;
- d) Annex C (Calculations of time dependent probabilities), Annex D (Importance factors), Annex E (RBD driven Petri net models) and Annex F (Numerical examples and curves) have been introduced.

The text of this standard is based on the following documents:

FDIS	Report on voting
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Full information on the voting for the approval of this standard can be found in the report on voting indicated in the above table.

This publication has been drafted in accordance with the ISO/IEC Directives, Part 2.

The committee has decided that the contents of this publication will remain unchanged until the stability date indicated on the IEC web site under "<http://webstore.iec.ch>" in the data related to the specific publication. At this date, the publication will be

- reconfirmed,
- withdrawn,
- replaced by a revised edition, or
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INTRODUCTION

A reliability block diagram (RBD) is a pictorial representation of a system's successful functioning. It shows the logical connection of (functioning) components (represented by blocks) needed for successful operation of the system (hereafter referred to as "system success"). Therefore an RBD is equivalent to a logical equation of Boolean variables and the probabilistic calculations are primarily related to constant values of the block success/failure probabilities.

Many different analytical methods of dependability analysis are available, of which the RBD is one. Therefore, the purpose of each method and their individual or combined applicability in evaluating the availability, reliability, failure frequency and other dependability measures as may be applicable to a given system or component should be examined by the analyst prior to deciding to use the RBD. Consideration should also be given to the results obtainable from each method, data required to perform the analysis, complexity of analysis and other factors identified in this standard.

Provided that the blocks in the RBD behave independently from each other and that the order in which failures occur does not matter then the probabilistic calculations can be extended to time dependent probabilistic calculations involving non-repaired as well as repaired blocks (e.g. blocks representing non-repaired or repaired components). In this case three dependability measures related to the system successful functioning have to be considered: the reliability itself, $R_S(t)$, but also the availability, $A_S(t)$ and the failure frequency, $w_S(t)$. While, for systems involving repaired components, the calculations of $A_S(t)$ or $w_S(t)$ can be done quite straightforwardly, the calculation of $R_S(t)$ implies systemic dependencies (see definition 3.34) which cannot be taken into account within the mathematical framework of RBDs. Nevertheless, in particular cases, approximations of $R_S(t)$ are available.

The RBD technique is linked to fault tree analysis [1]¹ and to Markov techniques [2]:

- The underlying mathematics is the same for RBDs and fault tree analysis (FTA): when an RBD is focused on system success, the FT is focused on system failure. It is always possible to transform an RBD into an FT and vice versa. From a mathematical point of view, RBD and FT models share dual logical expressions. Therefore, the mathematical developments and the limitations are similar in both cases.
- When the availability $A_i(t)$ of one block can be calculated by using an individual Markov process [2] independent of the other blocks, this availability, $A_i(t)$, can be used as input for the calculations related to an RBD including this block. This approach where an RBD provides the logic structure and Markov processes numerical values of the availabilities of the blocks is called "RBD driven Markov processes".

For systems where the order of failures is to be taken into account, or where the repaired blocks do not behave independently from each other or where the system reliability, $R_S(t)$, cannot be calculated by analytical methods, Monte Carlo simulation or other modelling techniques, such as dynamic RBDs, Markov [2] or Petri net techniques [3], may be more suitable.

¹ Numbers in square brackets refer to the Bibliography.

RELIABILITY BLOCK DIAGRAMS

1 Scope

This International Standard describes:

- the requirements to apply when reliability block diagrams (RBDs) are used in dependability analysis;
- the procedures for modelling the dependability of a system with reliability block diagrams;
- how to use RBDs for qualitative and quantitative analysis;
- the procedures for using the RBD model to calculate availability, failure frequency and reliability measures for different types of systems with constant (or time dependent) probabilities of blocks success/failure, and for non-repaired blocks or repaired blocks;
- some theoretical aspects and limitations in performing calculations for availability, failure frequency and reliability measures;
- the relationships with fault tree analysis (see IEC 61025 [1]) and Markov techniques (see IEC 61165 [2]).

2 Normative references

The following documents, in whole or in part, are normatively referenced in this document and are indispensable for its application. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

IEC 60050-192, *International Electrotechnical Vocabulary – Part 192: Dependability* (available at <http://www.electropedia.org>)

IEC 61703, *Mathematical expressions for reliability, availability, maintainability and maintenance support terms*

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